

ALGEBRA – P16MS1

Semester : I
Instruction Hours/Week: 6

Core Course: I
Credit: 5

UNIT I

A Counting Principle – Permutation Groups – Another Counting Principle – Sylow's theorem - Direct Products.

UNIT II

More Ideals and Quotient Rings – Polynomial Rings – Polynomials over the Field – Polynomials over commutative Rings.

UNIT III

Dual Spaces - Inner Product Spaces – Modules.

UNIT IV

Extension fields – Roots of Polynomials – More about Roots.

UNIT V

The Elements of Galois Theory – Finite Fields.

TEXT BOOK

I.N. Herstein, Topics in Algebra, Second Edition, Wiley Eastern Limited.

UNIT I : Chapter 2 – Sections 2.5, 2.10, 2.11, 2.12, 2.13

UNIT II : Chapter 3 – Sections 3.5, 3.9, 3.10, 3.11

UNIT III : Chapter 4 – Sections 4.3, 4.4, 4.5

UNIT IV : Chapter 5 - Sections 5.1, 5.3, 5.5, 5.6

UNIT V : Chapter 7 – Section 7.1

REFERENCE BOOK(S)

[1] P.B. Bhattacharya, S.K. Jain and S.R. Nagpul, Second Edition, 2005, Cambridge University Press.

[2] Vijay, K. Khanna, and S.K. Bhambri, A Course in Abstract Algebra, Vikas Publishing House Pvt Limited, 1993.

[3] John, B. Fraleigh, A First Course in Abstract Algebra, Addison-Wesley Publishing company.

REAL ANALYSIS – P16MS2

Semester : I
Instruction Hours/Week: 6

Core Course: II
Credit: 5

UNIT I

The real and complex number systems: ordered sets – fields – the real field – the extended real number system - the complex field – Euclidean spaces.

UNIT II

Basic Topology: finite, countable and uncountable sets – metric spaces – compact sets – perfect sets – connected sets.

UNIT III

Numerical sequences and series: convergent sequences – subsequences – Cauchy sequences – upper & lower limits – some special sequences – series – series of non negative terms – the number e – the root and ration tests – power series.

UNIT IV

Continuity: limits of functions – continuous functions – continuity and compactness – continuity and connectedness – discontinuities.

UNIT V

Differentiation: the derivative of a real function – mean value theorems – the continuity of derivative – L' Hospital's rule – derivatives of higher order.

TEXT BOOK

[1] Walter Rudin, Principles of Mathematical Analysis Third Edition, Mcgraw Hill, 1976.

UNIT I : Chapter 1 – Sections 1.1 – 1.38

UNIT II : Chapter 2 – Sections 2.1 – 2.47

UNIT III : Chapter 3 – Sections 3.1 – 3.40

UNIT IV : Chapter 4 – Sections 4.1 – 4.27

UNIT V : Chapter 5 – Sections 5.1 – 5.15

REFERENCE BOOKS(S)

[1] Simmons G.F, Topology and Modern Analysis, McGraw Hill Co. 1998.

[2] Apostol, Analysis Vol. II, Mac Millan 1976.

[3] A.T. White, Real Analysis : An Introduction, Addison Wesley Publishing Co., Inc.1968.

C++ PROGRAMMING THEORY - P16MS3

Semester : I
Instruction Hours/Week: 6

Core Course: III
Credit: 5

UNIT I

Principles of object-Oriented Programming: Software crisis – Software evolution– A look at procedure-oriented Programming – Object-oriented Programming Paradigm – Basic Concepts of Object- Oriented Programming – Benefits of OOP – Object-Oriented languages – Applications of OOP.

UNIT II

Tokens, Expressions and Control structure: Introduction – Tokens – Keywords – Identifiers – basic data types – User defined data types - Derived data types – Symbolic constants – type compatibility – Declaration of variables – Dynamic initialization of variables – Reference variables – operations in C++ - Scope resolution operator – member Dereferencing operators – memory management operators – Manipulators – type cast operator – expressions and implicit conversions – Operator overloading – Operator Precedence – Control structures.

UNIT III

Functions in C++: Introduction – The main function – Function prototyping – call by reference – return by reference inline functions – default arguments – const arguments – function overloading – friend and virtual functions – Managing Console I/O operations: Introduction – C++ streams – C++ stream classes – Unformatted I/O operations - Formatted console I/O operations – Managing output with manipulators.

UNIT IV

Classes and Objects: Introduction – C Structures Revisited – Specifying a class – Defining Member Functions – A C++ Program with class – Making an outside Function Inline – Nesting of Member Functions – Private Member Functions – Arrays within a class – Memory Allocation for Objects – Static Data Members – Static Member Functions – Arrays of Objects – Objects as Function Arguments – Friendly functions – Returning Objects – Const Member Functions. Constructors and Destructors: Introduction – Constructors – Parameterized Constructors – Multiple Constructors in a class – Constructors with Default Arguments – Dynamic Initializations of Objects – Copy Constructor – Constructing Two dimensional arrays – Destructors.

UNIT V

Operator Overloading and Type Conversions: Introduction – Defining Operator Overloading – Overloading Unary Operators – Overloading Binary Operators – Overloading Binary Operators Using Friends – manipulation of strings using Operators – Rules of Overloading Operators. Inheritance: Extending Classes: Introduction – Defining Derived Classes – Single inheritance – Making a Private Member Inheritable – Multilevel Inheritance – Multiple Inheritance – Hierarchical Inheritance – Hybrid Inheritance – Virtual Base Classes –Abstract Classes – Constructors in Derived Classes – Member Classes: Nesting of Classes.

TEXT BOOK: Object – Oriented Programming with C++ by E. Balaguruswamy, Tata McGraw-Hill Publishing Company Limited, 1999.

- UNIT I** : Chapter 1 1.1 – 1.8
- UNIT II** : Chapter 3 3.1 – 3.24
- UNIT III** : Chapter 4 4.1 – 4.11 and 10.1 – 10.6
- UNIT IV** : Chapter 5 5.1 – 5.17, 6.1 – 6.7 and 6.9 – 6.10
- UNIT V** : Chapter 7 7.1 – 7.7 and 8.1 – 8.12

C++ PROGRAMMING LAB – P16MS4P

Semester : I
Instruction Hours/Week: 6

Core Course: IV
Credit: 5

1. DISTANCE CONVERSION PROBLEM:

Create two classes DM and DB which store the value of distances. DM stores distances in meters and centimeters in DB in feet and inches. Write a Program that can create the values of the class objects and add one object of DM with another object DB. Use a friend function to carry out addition operation. The object that stores the result may be DM object or DB object depending on the units in which results are required. The display should be in the order of meter and centimeter or feet and inches depending on the order of display.

2. OVERLOADING OBJECTS:

Create a class FLOAT that contains one float data member overload all the four arithmetic operators so that operate on the objects of FLOAT.

3. POLAR CONVERSION:

Define two classes polar and rectangular to represent points in the polar and rectangle systems. Use conversion routines to convert from one system to another.

4. OVERLOADING CONVERSIONS:

Add two points in polar coordinates using overloading + .

5. OVERLOADING MATRIX:

Create a class MAT of size M*N. Define all possible matrix operations for MAT type objects. Verify the identity $(A-B)^2 = A^2 + B^2 - 2*A*B$.

6. AREA COMPUTATION USING DERIVED CLASS:

Area of rectangle = $X*Y$

Area of triangle = $(\frac{1}{2}) * X * Y$

7. VECTOR PROBLEM:

Define a class for vector containing scalar values. Apply overloading concepts for vector addition, Multiplication of a vector by a scalar quantity, replace the values in a position vector.

COMPLEX ANALYSIS – P16MS6

Semester : II
Instruction Hours/Week: 6

Core Course: VI
Credit: 5

UNIT – I

Fundamental theorems and Cauchy's Integral formula: Line Integrals- Rectifiable Arcs – Line Integrals as Functions of Arcs-Cauchy's Theorem for a Rectangle-Cauchy's Theorem in a Disk. The Index of a point with Respect to a closed curve-The Integral Formula – Higher Derivatives.

UNIT – II

Local properties of Analytical Functions : Removable Singularities – Taylor's Theorem - Zeros and Poles - The Local Mapping - The Maximum Principle.

UNIT – III

The General Form of Cauchy's Theorem & The Calculus of residues: Chains and Cycles Simple Connectivity-Homology The General Statement of Cauchy's Theorem - Proof of Cauchy's Theorem-Locally Exact Differentials –Multiply Connected Regions.The Residue Theorem- The Argument Principle-Evaluation of Definite Integrals.

UNIT – IV

Harmonic Functions and Power series expansions: Definition and Basic Properties-The Mean value Property-Poisson's Formula-Schwarz's Theorem-The Reflection Principle. Weierstrass's Theorem-The Taylor Series-The Laurent Series.

UNIT – V

Partial fractions and factorization & Entire fractions: Partial fractions – Infinite products - Canonical products – The Gamma function. Jensen's formula - Hadamard's theorem.

Text Book(s)

Complex Analysis: Lars.V.Ahlfors, McGraw Hill Company-1979

Unit I : Chapter 4: 1.1-1.5, 2.1 – 2.3

Unit II : Chapter 4: 3.1,3.2,3.3,3.4

Unit III : Chapter 4: 4.1-4.7,5.1-5.3

Unit IV : Chapter 4: 6.1-6.5 and Chapter 5: 1.1-1.3

Unit V : Chapter 5: 2.1 to 2.4 :3.1, 3.2

Reference Book(s)

[1] Serge Lang, Complex Analysis,Addison Wesley, 1977

[2] S.Ponnisamy, Foundations of Complex Analysis, Narosa Publishing House, New Delhi 1997.

[3] V.Karunakaran, Complex Analysis

MEASURE AND INTEGRATION- P16MS7

Semester : II
Instruction Hours/Week: 6

Core Course: VII
Credit: 5

UNIT – I

Measure on Real line: Lebesgue outer measure – Measurable sets – Regularity- Measurable functions – Borel and Lebesgue measurability.

UNIT – II

Integration of Functions of Real variable: Integration of non-negative functions – The General Integral – Integration of series – Riemann and Lebesgue integrals.

UNIT – III

Abstract Measure spaces: Measures and outer measures – completion of a measure – Extension of a measure – uniqueness of the extension - Measure spaces – Integration with respect to a measure.

UNIT – IV

Convergence in Measure – Almost uniform convergence - Signed Measures and Hahn Decomposition – The Jordan Decomposition.

UNIT – V

Measurability in a product space – The product Measure and Fubini's Theorem.

Text Book(s)

G.De Barra , Measure Theory and Integration, New age international (P) Limited.

- Unit I** : Chapter II: Sections 2.1 to 2.5
Unit II : Chapter III: Sections 3.1 to 3.4
Unit III : Chapter V: Sections 5.1 to 5.6
Unit IV : Chapter VII: Sections 7.1 and 7.2,
Chapter VIII: Sections 8.1 and 8.2
Unit V : Chapter X: Sections 10.1 and 10.2

Reference(s)

- [1] Measure and Integration, by M.E.Munroe, Addison – Wesley publishing company, Second Edition, 1971.
[2] P.K.Jain, V.P.Gupta, Lebesgue Measure and integration, New Age International Pvt Limited Publishers, New Delhi, 1986. (Reprint 2000)
[3] Richard L.Wheeden and Antoni Zygmund, Measure and Integral: An Introduction to Real Analysis, Marcel Dekker Inc.1977.
[4] Inder, K.Rana, An Introduction to Measure and Integration, Narosa Publishing House, New Delhi, 1997.

ORDINARY DIFFERENTIAL EQUATIONS– P16MS8

Semester : II
Instruction Hours/Week: 6

Core Course: VIII
Credit: 5

UNIT – I

The general solution of the homogeneous equation – The use of one known solution to find another – The method of variation of parameters power Series solutions. A review of Power series – Series solutions of first order equations Second order linear equations: Ordinary points.

UNIT – II

Regular Singular points- Gauss's hypergeometric equation – The point at infinity- Legendre Polynomials – Bessel functions – Properties of Legendre Polynomials and Bessel functions.

UNIT – III

Linear Systems of First Order Equations – Homogeneous Equations with Constant Coefficients – The Existence and Uniqueness of Solutions of Initial value problem for First Order Ordinary Differential Equations – The Method of Solutions of Successive Approximations and Picard's Theorem.

UNIT – IV

Oscillation Theory and Boundary value problems – Qualitative Properties of Solutions – Sturm comparison Theorems – Eigen values, Eigen functions and the vibrating string.

UNIT – V

Nonlinear equations: Autonomous Systems: the phase plane and its phenomena Types of critical points: Stability – critical points and stability for linear systems Stability by Liapunov's direct method – Simple critical points of nonlinear systems.

Text Book (s)

G.F.Simmons, Differential Equations with Applications and Historical Notes, TMH , New Delhi, 1994.

Unit I : Chapter 3: Sections 15, 16,19 and Chapter 5: Sections 25 to 27.

Unit II : Chapter 5: Sections 28 to 31 and Chapter 6: Sections 32 to 35

Unit III : Chapter 7: Sections 37,38 and Chapter 11: Sections 55,56

Unit IV : Chapter 4: Sections 22 to 24

Unit V :Chapter 8: Sections 42 to 44.

References

[1] W.T.Rcid, Ordinary Differential Equations, John Wilcy & Sons, New York, 1971.

[2] E.A.Coddington and N.Levinson, Theory of Ordinary Differential Equations, McGraw Hill Publishing Company, New York, 1955.

CORE COURSE VIII - CLASSICAL DYNAMICS- P16MS9

Semester : II
Instruction Hours/Week: 6

CoreCourse:IX
Credit: 5

UNIT – I

Introductory concepts: The mechanical system – Generalized Coordinates –constraints – virtual work – Energy and momentum.

UNIT – II

Lagrange's equation: Derivation of Lagrange's equation and examples – Integrals of the Motion – Small oscillations.

UNIT – III

Special Applications of Lagrange's Equations: Rayleigh's dissipation function – impulsive motion – Gyroscopic systems – velocity dependent potentials.

UNIT – IV

Hamilton's equations: Hamilton's Principal – Hamilton's equations – Other variational principles – phase space.

UNIT – V

Hamilton – Jacobi Theory: Hamilton's Principal Function – The Hamilton – Jacobi equation – Separability.

Text Book (s)

Classical Dynamics, Donald T.Greenwood, PH1 Pvt. Ltd., New Delhi-1985.

Unit I : Chapter 1: Sections 1.1 to 1.5

Unit II : Chapter 2: Sections 2.1 to 2.4

Unit III : Chapter 3: Sections 3.1 to 3.4

Unit IV : Chapter 4: Sections 4.1 to 4.4

Unit V : Chapter 5: Sections 5.1 to 5.3

Reference (s)

[1] Herbert Goldstein, classical Mechanics, (2nd edition), Narosa Publishing House, New Delhi.

[2] Narayan Chandra Rana & Prmod Sharad Chandra Joag, Classical Mechanics, Tata McGraw Hill, 1991.

CORE COURSE IX – TOPOLOGY – P16MS11

Semester : III
Instruction Hours/Week: 6

Core Course: XI
Credit: 5

UNIT – I

TOPOLOGICAL SPACES: Basis for a topology – The order topology – The product topology on $X \times Y$ – The subspace topology – closed sets and limit points.

UNIT – II

CONTINUOUS FUNCTIONS: Continuous functions – the product topology – The metric topology.

UNIT – III

CONNECTEDNESS: Connected spaces – connected subspaces of the real line – Components and local connectedness.

UNIT – IV

COMPACTNESS: Compact spaces – compact subspaces of the Real line – Limit point compactness – Local compactness.

UNIT – V

COUNTABILITY AND SEPARATION AXIOMS: The countability Axioms – The separation Axioms – Normal spaces – Statements of the Urysohn Lemma, the Urysohn metrization Theorem and the Tietz extension(Proofs are not needed).

Text Book(S)

James R. Munkres, **Topology (2nd Edition) Pearson Education Pvt. Ltd., New Delhi-2002.(Third Indian Reprint)**

- Unit I** : Chapter 2: Sections 12 to 17.
Unit II : Chapter 2: Sections 18 to 21 (Omit Section 22).
Unit III : Chapter 3: Sections 23 to 23.
Unit IV : Chapter 3: Sections 26 to 29.
Unit V : Chapter 4: Sections 30 to 35.

REFERENCE(S)

- [1] J. Dugundji, Topology, Prentice Hall of India, New Delhi, 1975.
[2] George F. Simmons, Introduction to Topology and Modern Analysis, McGraw Hill Book Co., 1963.
[3] J.L. Kelly, General Topology, Van Nostrand, Reinhold Co., New York.
[4] L. Steen and J. Seebach, Counter examples in Topology, Holt, Rinehart and Winston, New York, 1970.

PARTIAL DIFFERENTIAL EQUATIONS – P16MS12

Semester : III
Instruction Hours/Week: 6

Core Course: XII
Credit: 5

UNIT – I

First order P.D.E.- Curves and Surfaces – Genesis of First Order P.D.E. – Classification of Integrals – Linear Equations of the first order – Pfaffian Differential Equations – Compatible systems – Charpit's Method – Jacobi's Method.

UNIT – II

Integral Surfaces Through a given Curve – Quasi – Linear Equations – Non-Linear First Order P.D.E.

UNIT – III

Second order P.D.E: Genesis of second order P.D.E. – Classification of Second order P.D.E. One – Dimensional Wave equation – vibrations of an infinite string – Vibrations of semi-infinite string – Vibrations of a String of Finite Length (Method of separation of variables)

UNIT – IV

Laplace's Equation: Boundary value Problems – Maximum and Minimum Principles – The Cauchy Problem – The Dirichlet problem for the Upper Half Plane – The Neumann Problem for the Upper Half Plane – The Dirichlet Interior Problem for a circle – The Dirichlet Exterior for a circle – The Neumann Problem for a circle – The Dirichlet Problem for a Rectangle – Harnack's Theorem – Laplace's Equation – Green's Function.

UNIT – V

Heat Conduction problem – Heat Conduction – Infinite Rod case - Heat Conduction finite Rod case – Duhamel's Principle – Wave Equation – Heat Conduction Equation.

Text Book(S)

An Elementary course in Partial Differential Equations By T. Amarnath, Narosa, 1997.

Unit – I – Chapter 1: Sections 1.1 to 1.8

Unit – II – Chapter 1: Sections 1.9 to 1.11.

Unit – III – Chapter 2: Sections 2.1 to 2.3.5, except 2.3.4.

Unit – IV – Chapter 2: Sections 2.4 to 2.4.11

Unit – V – Chapter 2: Sections 2.5 to 2.6.2.

REFERENCE(S)

1. I.c.Evans, Partial Differential Equations, Graduate Studies in Mathematics, Vol 19 AMS, 1998.

2. I.N.Snedden, Elements of Partial Differential Equations.

3. F.John , P.Prasad , Partial Differential Equations.

INTEGRAL EQUATIONS AND CALCULUS OF VARIATIONS – P16MS13

Semester : III
Instruction Hours/Week: 6

Core Course: XIII
Credit: 5

UNIT – I

Liner Integral Equations – Definition, Regularity conditions – special kind of kernels – Eigen values and eigen functions – Convolution Integral – The inner and scalar product of two functions – notation – Integral equations – Examples – Fredholm alternative – examples – an approximate method.

UNIT – II

Method of successive approximation: Iterative scheme – examples- Volterra Integral equation – examples – some results about the resolvent kernel.

UNIT – III

Classical Fredholm Theory: The method of solution of Fredholm – Fredholm's first theorem – second theorem – third theorem.

UNIT – IV

Applications to ordinary differential equations – Initial value problems – Boundary value problems – singular integral equations – Abel integral equation.

UNIT – V

Calculus of variation – Maxima and Minima – The simplest case – Natural boundary conditions and transition conditions – The Variational notation – The more general case with illustrative equations – Constraints and Lagrange's multipliers – Variable end points – Sturm – Liouville Problems.

Text Book(S)

[1] Ram.P.Kanwal-Linear Integral Equations Theory and Practise, Academic Press 1971.

[2] F.B.Hildebrand, Methods of Applied Mathematics II ed. PHI, ND 1972.

Unit – I – Chapter 1 and 2 of [1]

Unit – II – Chapter 3 of [1]

Unit – III – Chapter 4 of [1]

Unit – IV – Chapter 5 (5.1,5.2,5.3) and Chapter 8 (8.1, 8.2) of [1].

Unit – V – Chapter 2 Section 2.1 to 2.9 of [2]

REFERENCE(S)

[1] S.J.Mikhlin, Linear Integral Equations (translated from Russian), Hindustan Book Agency, 1960.

[2] I.N.Snedden, Mixed Boundary value Problems in Potential Theory, North Holland, 1966.

FUNCTIONAL ANALYSIS – P16MS16

Semester : IV

Instruction Hours/Week: 6

Core Course: XVI

Credit: 5

UNIT – I

Banach Spaces : The definition and some examples – Continuous linear transformations – The Hahn – Banach theorem – The natural imbedding of N in N^{**} - The open mapping theorem – The conjugate of an operator.

UNIT – II

Hilbert Spaces : The definition and some simple properties – Orthogonal complements – Orthonormal sets – The conjugate space H^* - The adjoint of an operator – Self-adjoint operators – Normal and Unitary operators – Projections.

UNIT – III

Finite-Dimensional Spectral Theory : Matrices – Determinants and the spectrum of an operator – The Spectral theorem – A survey of the situation.

UNIT – IV

General Preliminaries on Banach Algebras : Definition and examples – Regular and singular elements – Topological divisors of zero – The spectrum – The formula for the Spectral radius – The radical and semi simplicity.

UNIT – V

The Structure of Commutative Banach Algebras : The Gelfand mapping – Applications of the formula $r(x) = \lim \|x^n\|^{1/n}$ – Involutions in Banach Algebras – The Gelfand – Neumark theorem.

TEXT BOOK (S)

Introduction to Topology and Modern Analysis, G.F. Simmons, Tata McGraw- Hill Publishing Company Limited, 2004.

UNIT I : Chapter 9

UNIT II : Chapter 10

UNIT III : Chapter 11

UNIT IV : Chapter 12

UNIT V : Chapter 13

REFERENCE (S) :

[1] Walter Rudin, Functional Analysis, TMH Edition, 1974. [2] B.V. Limaye, Functional Analysis, Wiley Eastern Limited, Bombay, Second Print, 1985.

[3] K. Yosida, Functional Analysis, Springer – Verlag, 1974.

[4] Laurent Schwarz, Functional Analysis, Courant Institute of Mathematical Sciences, New York University, 1964.

FLUID DYNAMICS – P16MS17

Semester : IV
Instruction Hours/Week: 6

Core Course: XVII
Credit: 5

UNIT I :

Kinematics of fluids in motion – Real fluids and ideal fluids, velocity of a fluid at a point streamlines and pathlines, Steady and unsteady flows. The Velocity potential, the vorticity vector, Local and particle rates of change, The equation of continuity, worked examples, acceleration of a point of a fluid.

UNIT II :

Equations of motion of a fluid-pressure at a point in a fluid at rest, Pressure at a point in a moving fluid, Condition at a boundary of two in viscid, Immissible fluids, Euler's equations of motion, worked examples, Some flows involving axial symmetry, Some special two dimensional flows, Impulsive motion.

UNIT III :

Some three dimensional flows – Introduction, sources, sinks and doublets, images in a rigid infinite plane. Axi-symmetric flows, stokes stream function, some special form of the stream function for axi-symmetric irrotational motions.

UNIT IV :

Some two dimensional flows- Meaning of two dimensional flow, use of cylindrical polar coordinates, The stream function. The complex potential for two-dimensional irrotational, incompressible flow, complex velocity potential for standard two-dimensional flows, uniform stream, line sources and line sinks, line doublets, line vortices, worked examples.

UNIT V :

Two dimensional image systems, The Milne Thomson circle Theorem, some application of the circle theorem, extension of the circle theorem, the theorem of Blasius, The use of conformal transformation- Some hydro dynamical aspects of conformal transformation worked example, vortex rows- single infinite rows of line vortices, The Karman vortex street.

TEXT BOOK (S) :

"FLUID DYNAMICS" F. Chorlton (CBS Publishers the distributors, New Delhi – 110032) 1985.

UNIT I: Chapter 2 Section 2.1 to 2.9

UNIT II: Chapter 3 Section 3.1 to 3.6, 3.9 to 3.11

UNIT III: Chapter 4 Section 4.1 to 4.3, 4.5, 4.5.1

UNIT IV: Chapter 5 Section 5.1 to 5.6

UNIT V: Chapter 5 Section 5.7 to 5.10.2, 5.12 to 5.12.2

REFERENCE BOOK:

Fluid Dynamics, Raisinghania.M.D.

NUMERICAL ANALYSIS – P16MS5E

Semester: I
Instruction Hours/Week: 6

Elective Course: I
Credit: 4

UNIT – II

Transcendental and polynomial equations: Muller method , Chebyshev method – Multipoint iteration method - Rate of convergence - Iteration methods. Polynomial equations: Birge-Vieta method, Bairstow's method, Graeffe's root squaring method only.

UNIT – II

System of Linear Algebraic equations and Eigen Value Problems: Decomposition method, Partition method - Error Analysis of direct and iteration methods – Finding eigen values and eigen vectors – Jacobi and Power methods.

UNIT – II

Interpolation and Approximation : Hermite Interpolations – Piecewise and Spline Interpolation – Bivariate Interpolation- Approximation – Least square approximation.

UNIT – IV

Differentiation and Integration: Numerical Differentiation - Optimum choice of Step length – Extrapolation methods – Partial Differentiation – Methods based on undetermined coefficients – Gauss-Legendre integration method and Lobatto, Radau, Gauss – Chebyshev integration methods only – Double integration.

UNIT – V

Ordinary differential equations: Introduction, Euler, Backward Euler, Mid-point, Taylor series method - Runge-Kutta methods – Stability analysis with single step methods only.

TEXT BOOK:

M.K. Jain, S.R.K. Iyengar and R.K. Jain, Numerical Methods for Scientific and Engineering Computation, III Edition, New Age International (P) Ltd Publishers, 1993.

UNIT I Chapter 2 – 2.4(P 32- 34), 2.5, 2.6, 2.8

UNIT II Chapter 3 – 3.2(P 90-93, 95-99), 3.3, 3.4, 3.5

UNIT III Chapter 4 – 4.5 to 4.7, 4.9(upto P 199)

UNIT IV Chapter 5 – 5.2 to 5.5, 5.8(upto P 262) and 5.11

UNIT V Chapter 6 – 6.1,6.2, 6.3, 6.6(upto P 343).

REFERENCE BOOKS(S)

- 1.C.F.Gerald and P.O.Wheatley , Applied Numerical Analysis, Fifth Edition, Addison Wesley, (1998).
- 2.Samuel D.Conte, Carl. De Boor, Elementary Numerical Analysis, Mc Graw Hill International Edition 1983.
- 3.M.KJain, Numerical Solutions of Differential Equations, Second Edition, New Age International (P) Ltd., 1983.

PROBABILITY AND STATISTICS – P16MS5E

Semester: I
Instruction Hours/Week: 6

Elective Course: I
Credit: 4

UNIT – I

Probability: Definitions of probability – addition theorem – conditional probability – multiplication theorem – Bayes's theorem – Geometric probability – Random variables and their properties – discrete random variable – continuous random variable – probability distributions – joint probability distributions and their properties – transformation variables – mathematical expectations – probability generating functions

UNIT – II

Probability distributions / Discrete distributions: Binomial, Poisson, negative binomial distributions and their properties (definition, mean, variance, moment generating function, additive properties, fitting of the distribution). Continuous distributions: Uniform, normal, exponential distributions and their properties – curve fitting using principle of least squares

UNIT – III

Multivariate Analysis: Correlation - Correlation coefficient - Rank correlation- Regression Analysis - Multiple Regression – Attributes - Coefficient of Association - χ^2 -test for goodness of fit- test for independence.

UNIT – IV

Sample – populations – statistic – parameter – Sampling distribution – standard error- unbiasedness – efficiency – Maximum likelihood estimator – notion & interval estimation. Testing of Hypothesis: Formulation of Null hypothesis- critical region – level of significance – power of the test.

UNIT – V

Queuing theory: Queue description – characteristics of a queuing model – study state solutions of M/M/1; N Model.

TEXT BOOK(S)

1. T. Veerarajan, "Probability, Statistics and Random Process", Tata McGraw Hill.

REFERENCE(S)

[1] Kishore S. Trivedi, "Probability & Statistics with Reliability, Queuing and Computer Applications", Prentice Hall of India, 1999

FUZZY MATHEMATICS – P16MS5E

Semester : I
Instruction Hours/Week: 6

Elective Course: I
Credit: 4

UNIT – I

Fuzzy sets — Basic types — Basic concepts — α -cuts — Additional properties of α - cuts — Extension principle for Fuzzy Sets

UNIT – II

Operations on Fuzzy sets — Types of operations — Fuzzy complements — t-Norms — Fuzzy Unions — Combinations of operations

UNIT – III

Fuzzy Arithmetic — Fuzzy numbers — Arithmetic operations on intervals Arithmetic operations on Fuzzy numbers.

UNIT – IV

Fuzzy relations — Binary fuzzy relations — Fuzzy equivalence relations — Fuzzy compatibility relations — Fuzzy ordering relations — fuzzy morphisms.

UNIT – V

Fuzzy Relation Equations — General discussion — Problem partitioning — Solution method — Fuzzy Relation Equations based on Sup- \circ Compositions - Fuzzy Relation Equations based on inf- \circ Compositions.

TEXT BOOK

George J.Klir and Bo Yuan, Fuzzy Sets and Fuzzy Logic, Prentice Hall of India New Delhi, 2004.

REFERENCE(S)

- [1] H.J. Zimmermann, Fuzzy Set Theory and its Applications, Allied Publishers Limited, New Delhi, 1991.
- (2) G.J. Klir and B. Yuan, Fuzzy Sets and Fuzzy Logic, Prentice Hall of India, New Delhi, 1995.

LINEAR ALGEBRA – P16MS10E

Semester : II
Instruction Hours/Week: 6

Elective Course: II
Credit: 4

UNIT – I

Reduced echelon Matrices – Matrix Multiplication Invertible Matrices Vector spaces – Subspaces – Bases and Dimension – Coordinates – summary of row equivalence - Computations concerning Subspaces.

UNIT – II

The algebra of linear transformations – Isomorphism of Vector Spaces - Representations of transformations by Matrices – Linear functionals – The Double Dual – The Transpose of a linear Transformation.

UNIT – III

Algebras - The algebra of polynomials – Lagrange Interpolation – Polynomial Ideals - The prime factorization of a polynomial.

UNIT – IV

Characteristic values – Annihilating polynomials, Invariant subspaces Simultaneous triangulation and simultaneous Diagonalization.

UNIT – V

Direct-sum Decompositions - Invariant Direct sums – The Primary Decomposition Theorem – Cyclic subspaces and annihilators – the Jordan form.

Text Book

Kenneth Hoffman and Ray Kunze, Linear Algebra, Second Edition, Prentice-Hall of India Private Limited, New Delhi 1975.

Unit I : Chapter 1: 1.4, 1.5, 1.6
Chapter 2: 2.1 to 2.6
Unit II : Chapter 3: 3.1 to 3.7
Unit III : Chapter 4: 4.1 to 4.5
Unit IV : Chapter 6: 6.1 to 6.5
Unit V : Chapter 6: 6.6 to 6.8
Chapter 7: 7.1 and 7.3

Reference(s)

- [1] I.N.Herstein, Topics in Algebra, Wiley Eastern Limited, New Delhi
- [2] I.S.Luther and I.B.S.Passi, Algebra, Vol.I – Groups, Vol.II – Rings, Narosa Publishing House (Vol.I – 1996, Vol II – 1999)
- [3] N.Jacobson, Basic Algebra, Vols.I & II, Freeman, 1980 (also published by Hindustan Publishing Company)

METHODS OF MATHEMATICAL PHYSICS– P16MS10E

Semester : II
Instruction Hours/Week: 6

Elective Course: II
Credit: 4

UNIT I

Boundary value problems and series solution - Examples of boundary value problems Eigen values, eigen functions and the Sturm-Liouville problem Hermitian operator, their eigen values and eigen functions.

UNIT II

Bessel functions Bessel functions of the second kind, Hankel functions Spherical Bessel functions - Legendre polynomials - Associated Legendre polynomials and spherical harmonics.

UNIT III

Hermite polynomials - Laguerre polynomials - The Gamma function The Dirac Delta function.

UNIT IV

Non homogeneous boundary value problems and Green's function - Green's function for one-dimensional problems – eigen function expansion of Greens function - Fourier transform method of constructing Greens function.

UNIT V

Green's function in higher dimensions - Green's function for Poisson's equation and a formal solution of electrostatic boundary value problems - Wave equation with source - the quantum mechanical scattering problem.

TEXT BOOK(S)

P.K. Chattopadhyay -Mathematical Physics, Wiley Eastern Limited, 1990

Unit I : Sections 4.2 to 4.5

Unit II : Sections 5.1 to 5.5

Unit III : Sections 5.6 to 5.9

Unit IV : Sections 6.1 to 6.4

Unit V : Sections 6.5. to 6.8.

REFERENCE(S)

[1] B.D. Gupta, Mathematical Physics, Vikas Publishing House Pvt Ltd, New Delhi, 1993.

[2] Goyal AK Ghatak, Mathematical Physics- Differential Equations and Transform Theory, McMillan India Ltd, 1995.

[3] Kryzeg, Higher Engineering Mathematics,

COMBINATORICS– P16MS10E

Semester : II
Instruction Hours/Week: 6

Elective Course: II
Credit: 4

UNIT I

Permutations and combinations - distributions of distinct objects — distributions of non distinct objects - Stirlings formula .

UNIT II

Generating functions. - generating function for combinations enumerators for permutations - distributions of distinct objects into non-distinct cells - partitions of integers - the Ferrers graphs elementary relations.

UNIT III

Recurrence relation - linear recurrence relations with constant coefficients solutions by the technique of generating functions – a special class of nonlinear difference equations recurrence relations with two indices.

UNIT IV

The principle of inclusion and exclusion - general formula -permutations with restriction on relative positions derangements - the rook polynomials permutations with forbidden positions.

UNIT V

Polya's theory of counting - equivalence classes under a permutation group Burnside theorem - equivalence classes of functions - weights and inventories of functions – Polya's fundamental theorem — generation of Polya's theorem.

TEXT BOOK(S)

C.L. Liu - Introduction of Combinatorial Mathematics, McGraw Hill, Chapters 1 to 5

REFERENCE(S)

[1] Marshall Hall. Jr., Combinatorial Theory

[2] H.J. Rayser, Combinatorial Mathematics, Carus, Mathematical Monograph, No14.

STOCHASTIC PROCESSES – P16MS14E

Semester : III
Instruction Hours/Week: 6

Elective Course: III
Credit: 4

Unit I

Stochastic Processes : Some notions – Specification of Stochastic processes – Stationary processes - Markov chains – Definitions and examples – Higher Transition probabilities – Generalization of Independent Bernoulli trails – Sequence of chain – Dependent trains.

Unit II

Markov chains: Classification of states and chains – determination of higher transition probabilities – stability of a Markov system – Reducible chains – Markov chains with continuous state space.

Unit III

Markov processes with Discrete state space: Poisson processes and their extensions – Poisson process and related distribution – Generalization of Poisson process – Birth and Death process – Markov system – Reducible chains – Markov chains with continuous state space.

Unit IV

Renewal processes and theory: Renewal processes - Renewal processes in continuous time - Renewal equation – stopping time – Wald's equation- Renewal theorems.

Unit V

Stochastic processes in Queuing – Queuing system – General concepts – the queuing model m/M/1 – Steady state Behaviour – transient behaviour of M/M/1 Model – Non-Markovian models – the model GI/M/1.

Text Book

J.Medhi, Stochastic Processes, Howard M. Taylor – Second Edition.

Unit I : Chapter 2 - Sec 2.1 to 2.3
Chapter 3 - Sec 3.1 to 3.3.

Unit II : Chapter 3 - Sec 3.4 to 3.6, 3.8,3.9 and 3.11.

Unit III : Chapter 4 - Sec 4.1 to 4.5.

Unit IV : Chapter 6 - Sec 6.1 to 6.5.

Unit V : Chapter 10 - Sec 10.1 to 10.3, 10.7 and 10.8 (omit 10.2.3 & 10.2.3.1)

REFERENCE(S)

- [1] Sameul Korlin, Howard M. Taylor, A first course in stochastic processes, II Edn.
- [2] Narayan Bhat, Elements of Applied Stochastic processes,
- [3] Srinivasan and Metha, Stochastic processes, N.V. Prabhu, Macmillan (NY), Stochastic Processes

OPERATOR THEORY- P16MS14E

Semester : III
Instruction Hours/Week: 6

Elective Course: III
Credit: 4

Unit I

Spectral theory of linear operators in normed spaces – spectral theory on finite dimensional normed spaces – basic concepts – special properties of bounded linear operators – properties of resolvent and spectrum- Banach algebra.

Unit II

Compact linear operators on normed spaces – properties – spectral properties of compact linear operators on normed spaces.

Unit III

Operator equations involving compact linear operators – Theorems of Fredholm type – Fredholm alternative.

Unit IV

Spectral properties of bounded self adjoint linear operators – positive operators square roots of a positive operator.

Unit V

Projection operators – their properties – spectral family – spectral family – spectral family of bounded self adjoint linear operators.

TEXT BOOK(S)

[1] Erwin Kreyszig-Introductory Functional Analysis, Springer – Verlag, 1974.

[2] L. S. Sobolev, Introduction to Linear Operators.

OPTIMIZATION TECHNIQUES – P16MS14E

Semester : III
Instruction Hours/Week: 6

Elective Course: III
Credit: 4

UNIT I

Integer programming

UNIT II

Dynamic (Multistage) programming.

UNIT III

Decision Theory and Games

UNIT IV

Inventory Models.

UNIT V

Non-Linear Programming algorithms.

TEXT BOOK(S)

Hamdy A.Taha, Operations Research (7th Edition), McGraw Hill Publications, New Delhi.

UNIT I	: Sections 8.1 to 8.5
UNIT II	: Sections 9.1 to 9.5
UNIT III	: Sections 11.1 to 11.4
UNIT IV	: Sections 13.1 to 13.4
UNIT V	: Sections 19.1 to 19.2

REFERENCES:

- [1] O.L.Mangasarian, Non Linear Programming, McGraw Hill, New York.
- [2] Mokther S.Bazaraa and C.M.Shetty, Non Linear Programming, Theory and Algorithms, Willy, New York.
- [3] Prem Kumar Gupta and D.S.Hira, Operations Research: An Introduction, S.Chand and Co., Ltd. New Delhi.
- [4] S.S.Rao, Optimization Theory and Applications, Wiley Eastern Limited, New Delhi.

DIFFERENTIAL GEOMETRY – P16MS15E

Semester : III
Instruction Hours/Week: 6

Elective Course:IV
Credit: 4

Unit I

Space Curves: Definition of a space curve – Arc length – Tangent – normal and binormal – curvature and torsion – contact between curves and surfaces – tangent surface – involutes and evolutes intrinsic equations – Fundamental Existence theorem for space curves – Helics.

Unit II

Intrinsic properties of a surface: Definition of a surface – curves on a surface – surface of revolution – Helicoids – Metric – Direction coefficients – families of curves – Isometric correspondence – Intrinsic Properties.

Unit III

Geodesics: Geodesics – canonical Geodesic equation – Normal property of Geodesics – (Existence theorem) – Geodesics Parallels – Geodesics curvature - Gauss Bonnet Theorem – Gaussian Curvature – surface of constant curvature.

Unit IV

Non intrinsic properties of a surface: The second fundamental form – Principal curvature - Lines of curvature – Developable associated with space curves and with curves on surface – Minimal surface – Ruled surfaces

Unit V

Differential geometry of surfaces: Compact surfaces whose points are umbilics – Hilbert's Lemma – Compact surfaces of constant curvature - Complete surface and their characterization – Hilbert's Theorem – conjugate points on geodesics.

Text Book(S)

T.J. Wilmore, An Introduction to Differential Geometry, Oxford University press, (17th Impression) New Delhi 2002. (Indian Print).

Unit I : Chapter I: Sections 1 to 9.
Unit II : Chapter II: Section 1 to 9.
Unit III : Chapter II: Section 10 to 18.
Unit IV : Chapter III: Section 1 to 8.
Unit V : Chapter IV: Section 1 to 8.

REFERENCE(S)

- [1] Struik, D.T. Lectures on classical Differential Geometry, Addison – Wesley, Mass. 1950.
- [2] Kobayashi S. and Nomizu.K. Foundations of Differential Geometry, InterScience publishers, 1963.
- [3] Wilhelm Klingenberg : A Course in Differential Geometry. Graduate Texts in Mathematics, Springer Verlag, 1978.
- [4] J.A.Thorpe Elementary topics in Differential Geometry, Under- Graduate Texts in Mathematics, Springer Verlag, 1979.

MATHEMATICAL MODELING– P16MS15E

Semester : III
Instruction Hours/Week: 6

Elective Course: IV
Credit: 4

UNIT I :

Introduction: Need, Techniques, Classifications and Characteristics of Mathematical Modeling – Mathematical Modeling through Geometry, Algebra, Trigonometry and Calculus.

UNIT II :

Mathematical Modeling through Ordinary Differential Equations of First order : Linear Growth and Decay Models – Non – Linear Growth and Decay models – Compartment models – Population Dynamics, Epidemics.

UNIT III :

Mathematical Modeling through Ordinary Differential Equations of Second Order: Planetary motions – Circular motion and motion of Satellites – Rectilinear motion – Electrical Circuits – Phillip’s Stabilization model for a Closed Economy – The Catenary – A Curve of Pursuit.

UNIT IV :

Mathematical modeling through Difference Equations : Simple models – Basic theory of linear difference equations with constant coefficients – Economics and Finance – Population Dynamics and Genetics – Probability theory.

UNIT V :

Mathematical modeling through graphs : Problems that can be modeled through graphs – directed graphs – Signed graphs – weighted digraphs – unoriented graphs.

TEXT BOOK :

J.N. Kapur, Mathematical Modeling, New Age International (P) Limited, Publishers, 1998.

UNIT I : Chapter 1 – Section 1.1 to 1.9

UNIT II : Chapter 2 – Section 2.1 to 2.4
Chapter 3 – Section 3.1, 3.2

UNIT III : Chapter 4 – Section 4.1 to 4.4

UNIT IV : Chapter 5 – Section 5.1 to 5.6

UNIT V : Chapter 7 – Section 7.1 to 7.5

REFERENCE:

J.N. Kapur, Mathematical Models in Biology and Medicine, Affiliated East – West Press Pvt Limited, New Delhi, 1981.

FINANCIAL MATHEMATICS - P16MS15E

Semester : IV
Instruction Hours/Week: 6

Elective Course: IV
Credit: 4

UNIT I

SINGLE PERIOD MODELS: Definition from Finance – Pricing a forward – One step Binary Model – A ternary model – Characterization of no arbitrage – Risk neutral probability measure.

UNIT II

BINOMIAL TREES AND DISCRETE PARAMETER MARTINGALES: Multiperiod Binary model – American options – Discrete parameter martingales and Markov processes - Martingale theorems – Binomial Representation theorem – Overturn to continuous models.

UNIT III

BROWNIAN MOTION: Definition of the process – Levy's Construction of Brownian Motion – The Reflection Principle and Scaling – Martingales in Continuous time.

UNIT IV

STOCHASTIC CALCULUS: Non-differentiability of Stock prices – Stock prices –Stochastic Integration-Ito's formula –Integration by parts and Stochastic Fubini theorem – Girsanov Theorem – Brownian Martingale Representation Theorem – Geometric Brownian Motion – The Feynman – Kac Representation.

UNIT V

BLOCK-SCHOLLES MODEL: Basic Block-Scholes Model – Block – Scholes price and Hedge for European Options-Foreign Exchange-Dividends-Bonds-market price of risk.

TEXT BOOK

Alison Etheridge, A course in Financial Calculus, Cambridge University Press, Cambridge 2002.

REFERENCES

- [1] Martin Baxter and Andrew Rennie, Financial Calculus: An introduction to Derivatives Pricing Cambridge University Press, Cambridge 1996.
- [2] Introduction to Stochastic Calculus Applied to Finance, Chapman and Hall, 1996.
- [3] Marek Musiela and Marek Rutkowski, Martingale Methods in Financial Modeling, Springer Verlag, New York, 1998.
- [4] Robert J Elliot and P.Ekkehard Kopp, Mathematics of Financial Markets, Springer Verlag, New York 2001.

APPLIED STATISTICS - P16MS18E

Semester : IV
Instruction Hours/Week: 6

Elective Course: V
Credit: 4

UNIT I :
STATISTICAL QUALITY CONTROL

UNIT II :
TIME SERIES ANALYSIS (Excluding the moving average mathematical treatment)

UNIT III :
INDEX NUMBERS

UNIT IV :
DEMAND ANALYSIS

UNIT V :
ANALYSIS OF VARIANCE

TEXT BOOK (S) :
S. C GUPTA AND V.K. KAPOOR FUNDAMENTALS OF APPLIED STATISTICS – THIRD EDITION, SULTAN CHAND & SONS

UNIT I : Chapter I - Sections 1.0 to 1.7
UNIT II : Chapter II - Sections 2.1 to 2.5
UNIT III : Chapter III - Sections 3.1 to 3.4
UNIT IV : Chapter IV - Section 4.1 to 4.7
UNIT V : Chapter V - Section 5.1 to 5.4

REFERENCE BOOK[s]:
D.R. Caze – APPLIED STATISTICS – Principle and examples
B.N. Ashana – APPLIED STATISTICS

NON LINEAR DIFFERENTIAL EQUATIONS – P16MS18E

Semester : IV
Instruction Hours/Week: 6

Elective Course: V
Credit: 4

Unit I:

First order systems in two variables and linearization: The general phase plane-some population models- Linear approximation at equilibrium points – Linear systems in matrix form.

Unit II:

Averaging Methods: An energy balance method for limit cycles- Amplitude and frequency estimates – Slowly varying amplitudes – nearly periodic solutions – periodic solutions: harmony balance – Equivalent linear equation by harmonic balance-Accuracy of a period estimate.

Unit III:

Perturbation Methods: Outline of the direct method – Forced Oscillations far from resonance-Forced Oscillations near resonance with Weak excitation – Amplitude equation for undamped pendulum – Amplitude Perturbation for the pendulum equation - Lindstedt's Method – Forced oscillation of a self –excited equation – The Perturbation Method and Fourier series.

Unit IV:

Linear Systems: Time Varying Systems –Constant coefficient System – Periodic Coefficients_ Floquet Theory – Wronskian.

Unit IV:

Stability: Poincare stability-solutions, paths and norms- Liapunov stability Stability of linear systems-Comparison theorem for the zero solutions of nearly –Linear systems.

References:

- [1] Differential Equations by G.F.Simmons,Tata McGraw Hill, New Delhi(1979)
- [2] Ordinary Differential Equations and Stability Theory by D.A.Sanchez, Freeman(1968).
- [3] Notes on Nonlinear Systems by J.K.Aggarwal, Van Nostrand,1972.251

TENSOR ANALYSIS AND SPECIAL THEORY OF RELATIVITY –P16MS18E

Semester : IV
Instruction Hours/Week: 6

Elective Course: V
Credit: 4

UNIT I

Invariance Transformations of coordinates and its properties Transformation by invariance - Transformation by covariance and contra variance - Covariance and contra variance - Tensor and Tensor character of their laws - Algebras of tensors - Quotient tensors - Symmetric and skew symmetric tensors - Relative tensors.

UNIT II

Metric Tensor - The fundamental and associated tensors - Christoffel's symbols - Transformations of Christoffel's symbols- Covariant Differentiation of Tensors - Formulas for covariant Differentiation- Ricci Theorem - Riemann -Christoffel Tensor and their properties.

Unit III

Einstein Tensor - Riemannian and Euclidean Spaces (Existence Theorem) – The e-systems and the generalized Kronecker deltas - Application of the e-systems.

UNIT IV

Special Theory of Relativity: Galilean Transformation - Maxwell's equations - The ether Theory — The Principle of Relativity Relativistic Kinematics : Lorentz Transformation equations – Events and simultaneity - Example Einstein Train - Time dilation – Longitudinal Contraction -Invariant Interval - Proper time and Proper distance — World line – Example - twin paradox - addition of velocities - Relativistic Doppler effect.

UNIT V

Relativistic Dynamics: Momentum - energy – Momentum energy four vector - Force - Conservation of Energy - Mass and energy - Example - inelastic collision - Principle of equivalence - Lagrangian and Hamiltonian formulations. Accelerated Systems : Rocket with constant acceleration - example - Rocket with constant thrust

TEXT BOOK(S)

- [1] I.S. Sokolnikoff, Tensor Analysis, John Wiley and Sons, New York, 1964
- [2] D. Greenwood, Classical Dynamics, Prentice Hall of India, NewDelhi, 1985
- UNIT I Chapter 2 : Sections 18 to 28 of [1]
- UNIT II Chapter 2 : Sections 29 to 37 of [1]
- UNIT III Chapter 2 : Section 38 to 41 of [1]
- UNIT IV Chapter 7 : Sections 7.1 and 7.2 of [2]
- UNIT V Chapter 7 : Sections 7.3 and 7.4 of [2]

REFERENCE(S)

- [1] J.L. Synge and A.Schild, Tensor Calculus, Toronto, 1949.
- [2] A.S. Eddington, The Mathematical Theory of Relativity, Cambridge University Press, 1930.
- [3] P.G. Bergman, An introduction to Theory of Relativity, New york, 1942,
- [4] G.E. Weatherburn, Riemannian Geometry and Tensor Calculus, Cambridge, 1938.